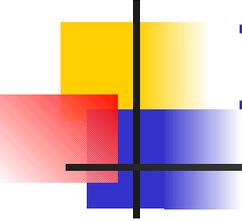


# Extending PDDL to Model Stochastic Decision Processes

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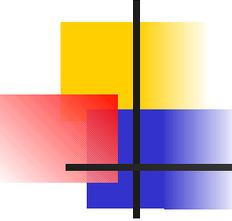
Håkan L. S. Younes  
Carnegie Mellon University



# Introduction

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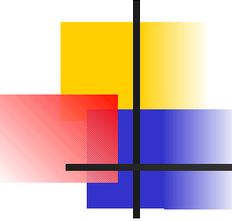
- PDDL extensions for modeling stochastic decision processes
  - Only full observability is considered
- Formalism for expressing probabilistic temporally extended goals
- No commitment on plan representation



# Simple Example

---

```
(:action flip-coin
  :parameters (?coin)
  :precondition (holding ?coin)
  :effect (and (not (holding ?coin))
               (probabilistic 0.5 (head-up ?coin)
                              0.5 (tail-up ?coin))))
```

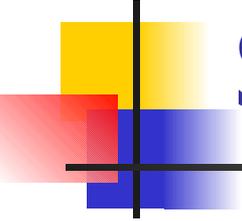


# Stochastic Actions

---

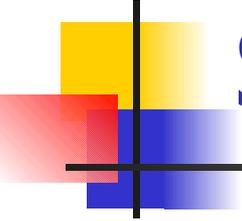
- Variation of factored probabilistic STRIPS operators [Dearden & Boutilier 97]
- An action consists of a precondition  $\phi$  and a consequence set  $C = \{c_1, \dots, c_n\}$
- Each  $c_i$  has a trigger condition  $\phi_i$  and an effects list  $E_i = \langle p_1^i, E_1^i; \dots; p_k^i, E_k^i \rangle$ 
  - $\sum_j p_j = 1$  for each  $E_i$

# Stochastic Actions: Semantics



---

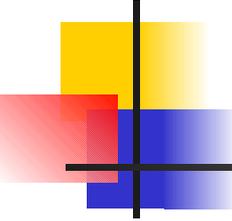
- An action is enabled in a state  $s$  if its precondition  $\phi$  holds in  $s$
- Executing a disabled action is allowed, but does not change the state
  - Different from deterministic PDDL
  - Motivation: partial observability
  - Precondition becomes factored trigger condition



# Stochastic Actions: Semantics (cont.)

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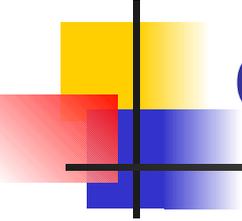
- When applying an enabled action to  $s$ :
  - Select an effect set for each consequence with enabled trigger condition
  - The combined effects of the selected effect sets are applied **atomically** to  $s$
  - Unique next state if consequences with mutually consistent trigger conditions have **commutative** effect sets



# Syntax of Probabilistic Effects

---

`<effect>` ::= `<d-effect>`  
`<effect>` ::= `(and <effect>*)`  
`<effect>` ::= `(forall (<typed list(variable)>) <effect>)`  
`<effect>` ::= `(when <GD> <d-effect>)`  
`<d-effect>` ::= `(probabilistic <prob-eff>+)`  
`<d-effect>` ::= `<a-effect>`  
`<prob-eff>` ::= `<probability> <a-effect>`  
`<a-effect>` ::= `(and <p-effect>*)`  
`<a-effect>` ::= `<p-effect>`  
`<p-effect>` ::= `(not <atomic formula(term)>)`  
`<p-effect>` ::= `<atomic formula(term)>`  
`<p-effect>` ::= `(<assign-op> <f-head> <f-exp>)`  
`<probability>` ::= *Any rational number in the interval [0, 1]*



# Correspondence to Components of Stochastic Actions

---

- Effects list:

(probabilistic  $p_1^i E_1^i \dots p_k^i E_k^i$ )

- Consequence:

(when  $\phi$  (probabilistic  $p_1^i E_1^i \dots p_k^i E_k^i$ ))

# Stochastic Actions: Example

(:action move

:parameters ()

:effect (and (when (office)

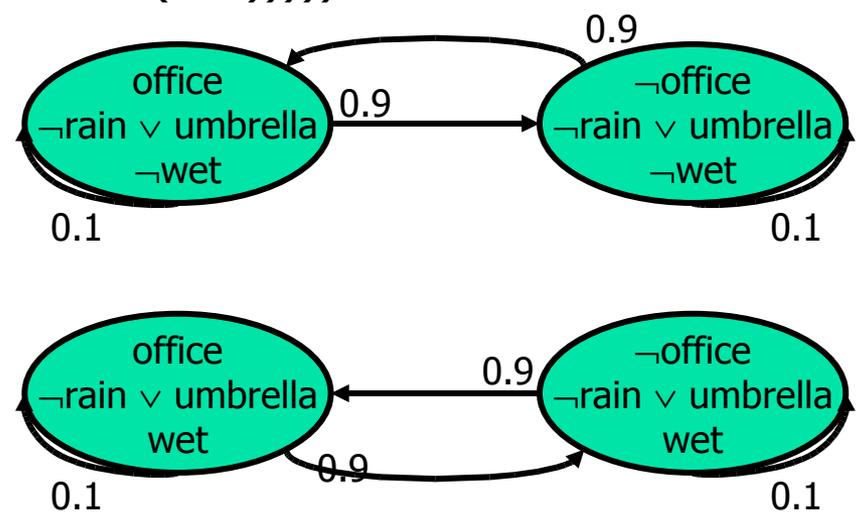
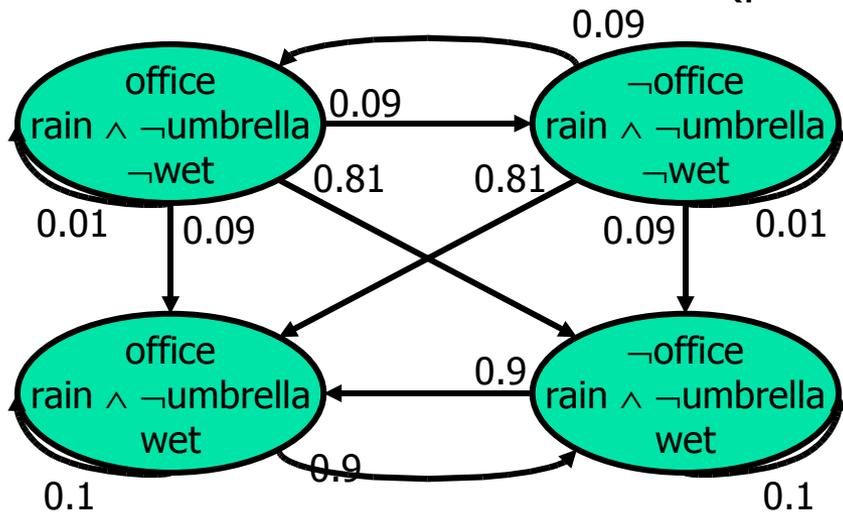
(probabilistic 0.9 (not (office))))

(when (not (office))

(probabilistic 0.9 (office))))

(when (and (rain) (not (umbrella)))

(probabilistic 0.9 (wet))))





# Stochastic Actions: Example

(:action move

:parameters ()

:effect (and (when (office)

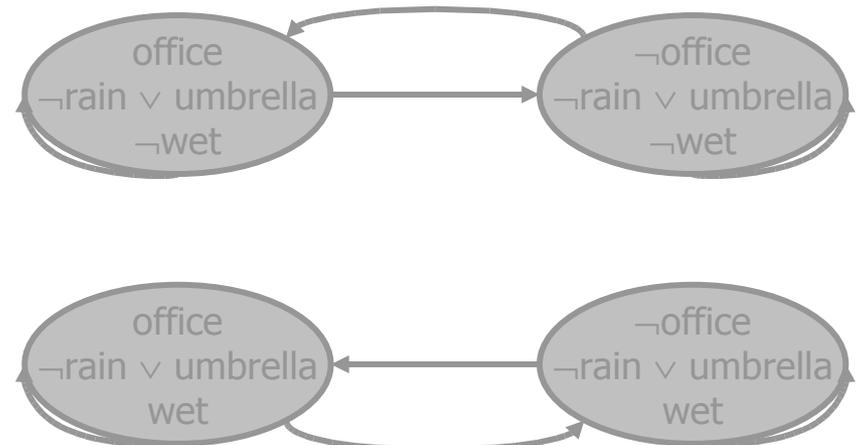
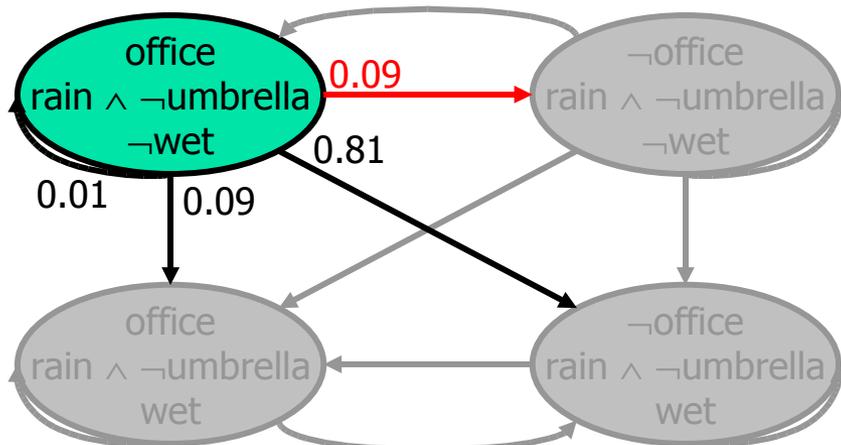
(probabilistic 0.9 (not (office)) 0.1 (and))))

(when (not (office))

(probabilistic 0.9 (office) 0.1 (and))))

(when (and (rain) (not (umbrella)))

(probabilistic 0.9 (wet) 0.1 (and))))))



# Stochastic Actions: Example

(:action move

:parameters ()

:effect (and (when (office)

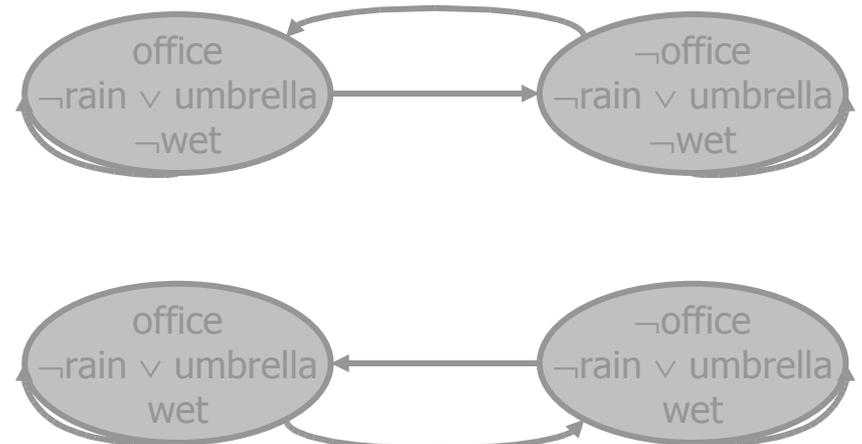
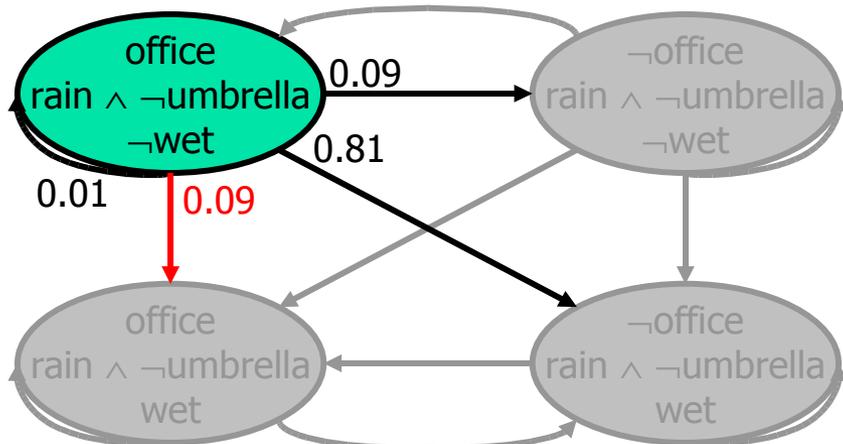
(probabilistic 0.9 (not (office)) **0.1 (and)**)))

(when (not (office))

(probabilistic 0.9 (office) 0.1 (and)))

(when (and (rain) (not (umbrella)))

(probabilistic **0.9 (wet)** 0.1 (and))))))



# Stochastic Actions: Example

(:action move

:parameters ()

:effect (and (when (office)

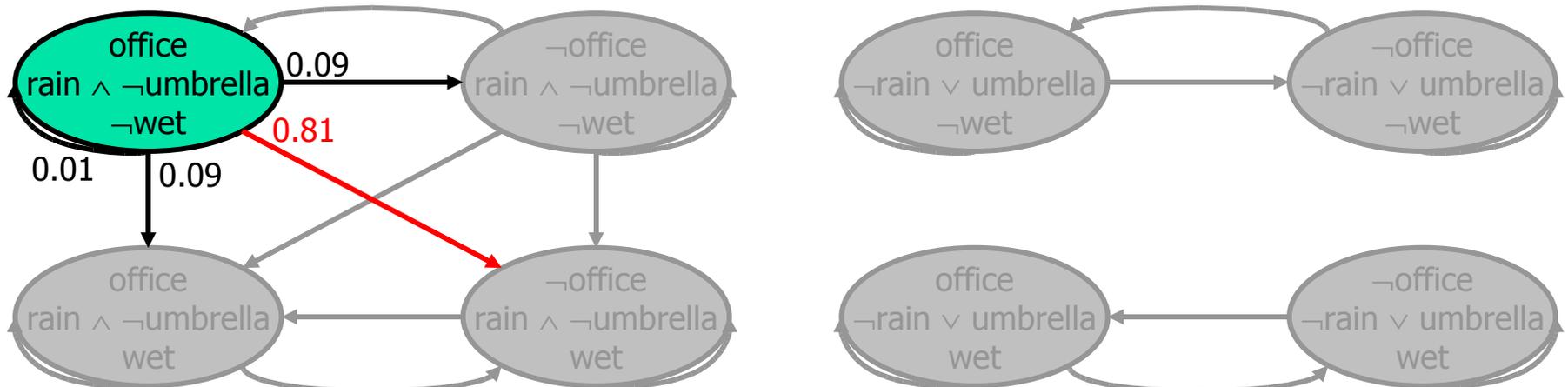
(probabilistic 0.9 (not (office)) 0.1 (and))))

(when (not (office))

(probabilistic 0.9 (office) 0.1 (and))))

(when (and (rain) (not (umbrella)))

(probabilistic 0.9 (wet) 0.1 (and))))))



# Stochastic Actions: Example

(:action move

:parameters ()

:effect (and (when (office)

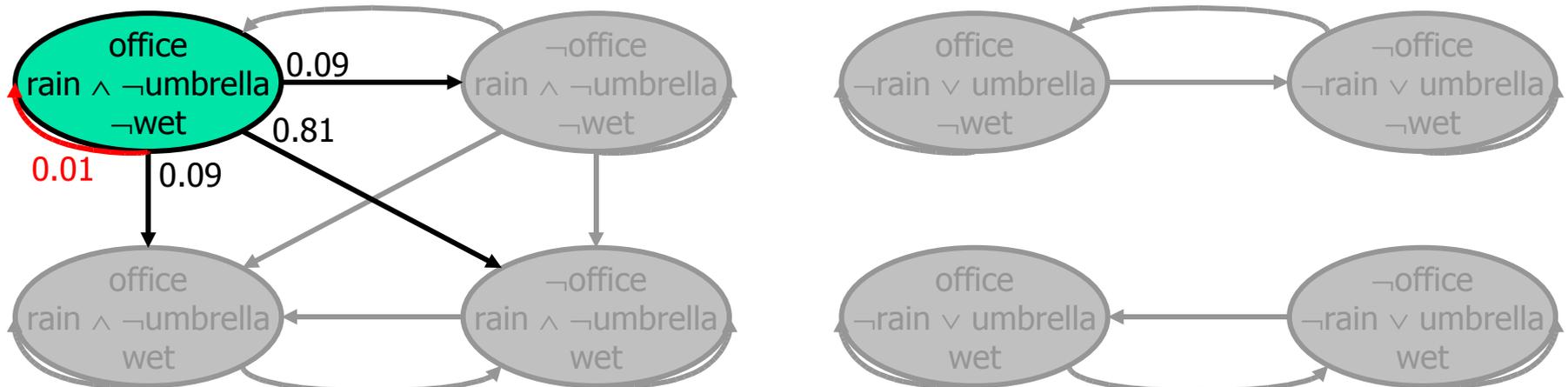
(probabilistic 0.9 (not (office)) **0.1 (and)**)))

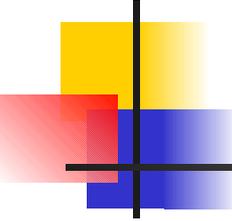
(when (not (office))

(probabilistic 0.9 (office) 0.1 (and)))

(when (and (rain) (not (umbrella)))

(probabilistic 0.9 (wet) **0.1 (and)**))))

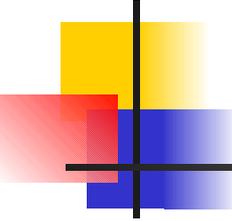




# Exogenous Events

---

- Like stochastic actions, but beyond the control of the decision maker
- Defined using `:event` keyword instead of `:action` keyword
- Common in control theory to say that everything is an event, and that some are controllable (what we call actions)



# Exogenous Events: Example

---

(:action move

:parameters ()

:effect (and (when (office)

(probabilistic 0.9 (not (office))))

(when (not (office))

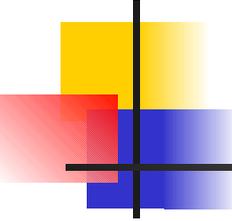
(probabilistic 0.9 (office))))))

(:event make-wet

:parameters ()

:precondition (and (rain) (not (umbrella)))

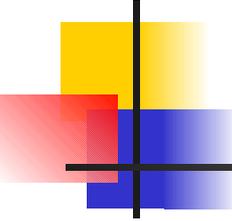
:effect (probabilistic 0.9 (wet)))



# Expressiveness

---

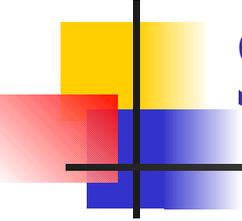
- Discrete-time MDPs
  - Exogenous events are so far only a modeling convenience and do not add to the expressiveness



# Adding Time

---

- States have stochastic duration
- Transitions are instantaneous



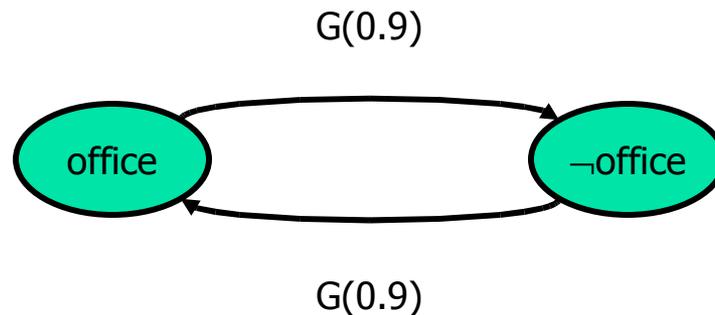
# Actions and Events with Stochastic Delay

---

- Associate a delay distribution  $F(t)$  with each action  $a$
- $F(t)$  is the cumulative distribution function for the delay from when  $a$  is enabled until it triggers
- Analogous for exogenous events

# Delayed actions and events: Example

```
(:delayed-action move  
  :parameters ()  
  :delay (geometric 0.9)  
  :effect (and (when (office) (not (office)))  
               (when (not (office)) (office))))
```



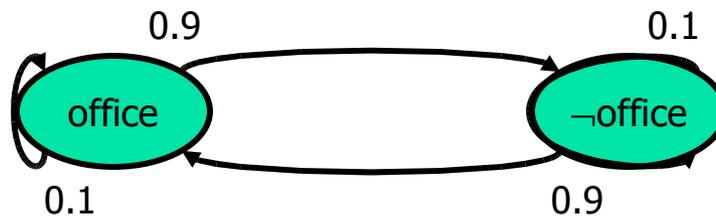
# Delayed actions and events: Example

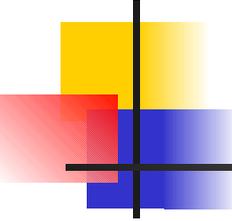
(:delayed-action move

:parameters ()

:delay (geometric 0.9)

:effect (and (when (office) (not (office)))  
(when (not (office)) (office))))



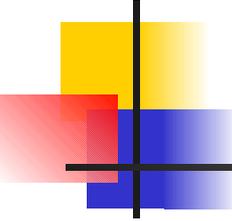


# Expressiveness

---

- Geometric delay distributions
  - Discrete-time MDP
- Exponential delay distributions
  - Continuous-time MDP
- General delay distributions
  - **At least** semi-Markov decision process

# General Delay Distribution: Example



---

(:delayed-action move

:parameters ()

:delay (uniform 0 6)

:effect (and (when (office) (not (office)))  
(when (not (office)) (office))))

(:delayed-event make-wet

:parameters ()

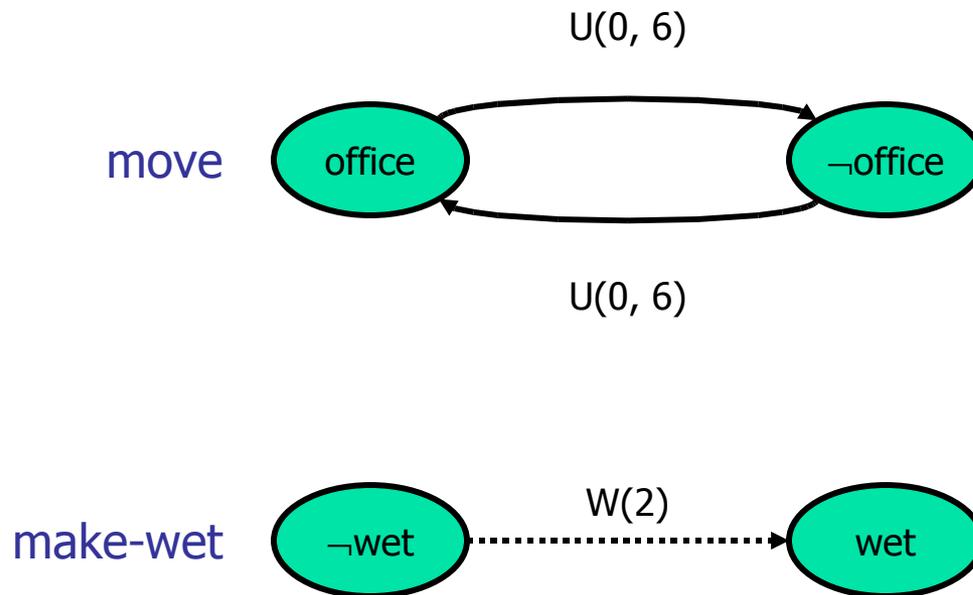
:delay (weibull 2)

:precondition (and (rain) (not (umbrella)))

:effect (wet))

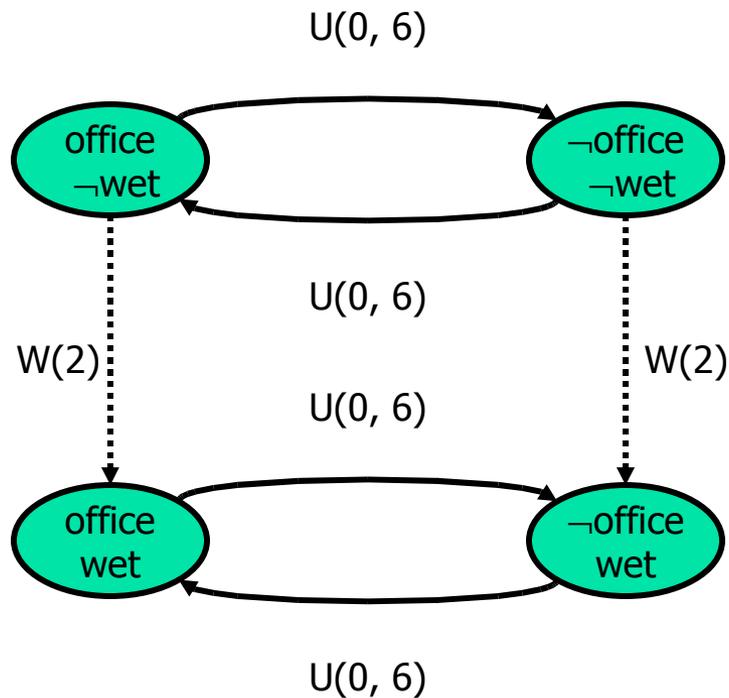
# Concurrent Semi-Markov Processes

- Each action and event separately



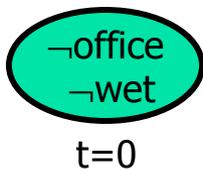
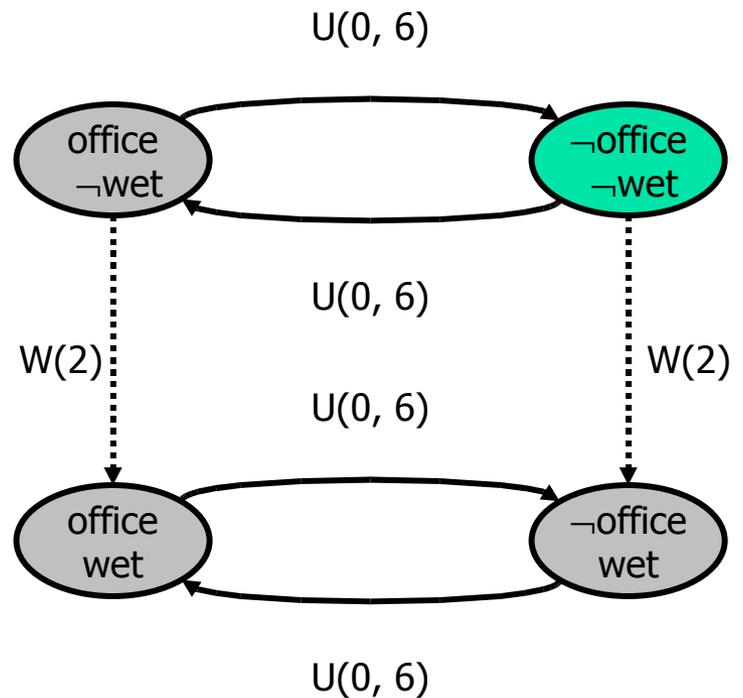
# Generalized Semi-Markov Process

- Putting it together



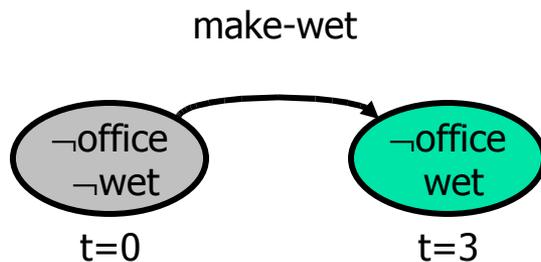
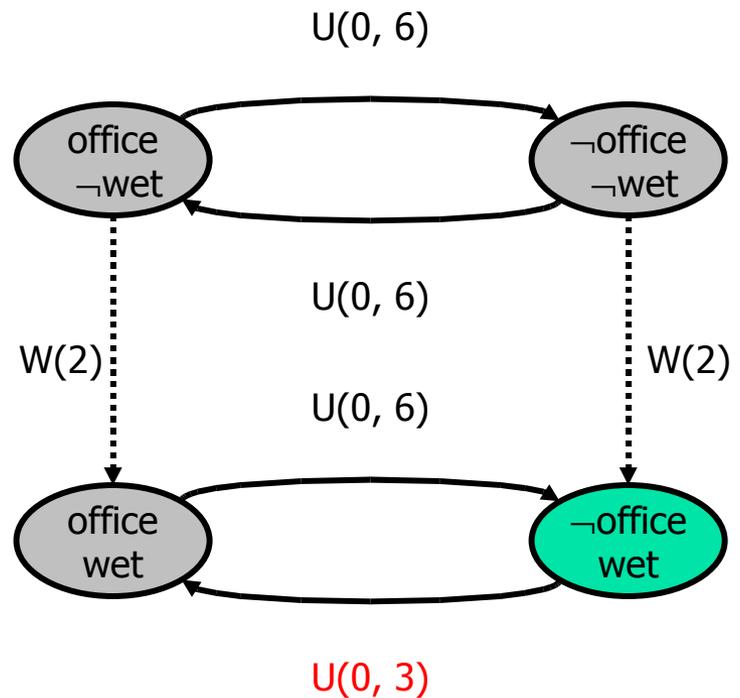
# Generalized Semi-Markov Process (cont.)

- Why **generalized**?



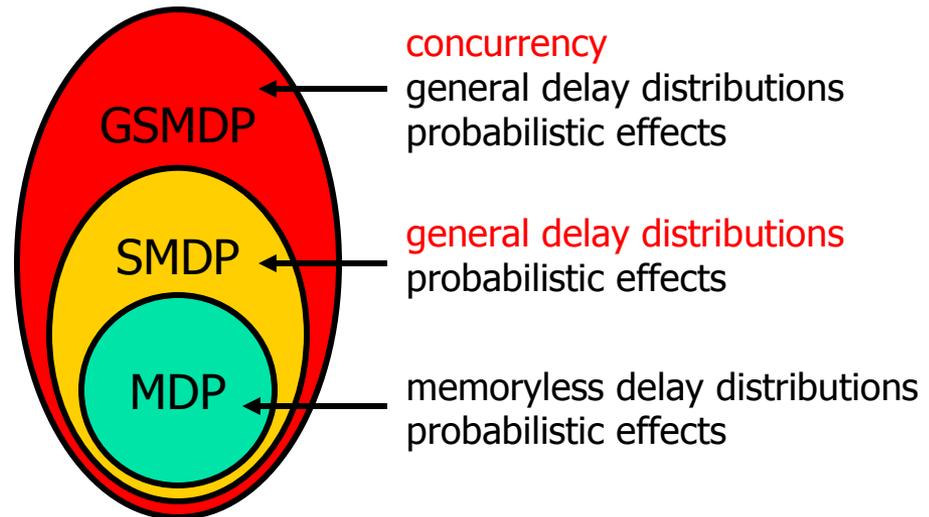
# Generalized Semi-Markov Process (cont.)

- Why generalized?



# Expressiveness

- Hierarchy of stochastic decision processes

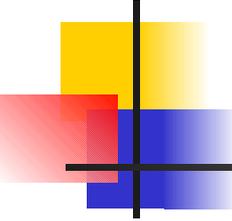


# Probabilistic

# Temporally Extended Goals

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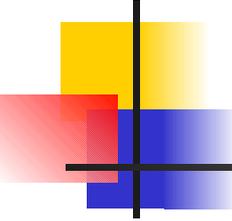
- Goal specified as a CSL (PCTL) formula
  - $\phi ::= \text{true} \mid a \mid \phi \wedge \phi \mid \neg\phi \mid \text{Pr}_{\sim p}(\rho)$
  - $\rho ::= \phi \text{ U}^{\leq t} \phi \mid \diamond^{\leq t} \phi \mid \square^{\leq t} \phi$



# Goals: Examples

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- Achievement goal
  - $\text{Pr}_{\geq 0.9}(\diamond \text{ office})$
- Achievement goal with deadline
  - $\text{Pr}_{\geq 0.9}(\diamond^{\leq 5} \text{ office})$
- Achievement goal with safety constraint
  - $\text{Pr}_{\geq 0.9}(\neg \text{wet} \text{ U office})$
- Maintenance goal
  - $\text{Pr}_{\geq 0.8}(\square \neg \text{wet})$

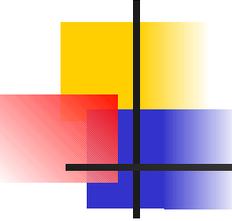


# Summary

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- PDDL Extensions
  - Probabilistic effects
  - Exogenous events
  - Delayed actions and events
- CSL/PCTL goals

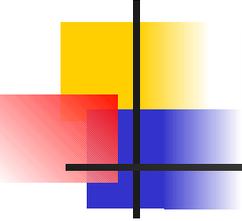
**Thursday:  
Planning!**



# Panel Statement

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- Stochastic decision processes are useful
  - Robotic control, queuing systems, ...
- Baseline PDDL should be designed with stochastic decision processes in mind
- Formalisms are needed to express complex constraints on valid plans
  - PCTL/CSL goals



# Role of PDDL

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